

Relativistic Mechanics

$$d\tau = \sqrt{1 - \frac{v^2}{c^2}} dt$$

τ = proper time, invariant

$$\vec{u} = \frac{d\vec{l}}{d\tau}, \quad \vec{v} = \frac{d\vec{l}}{dt} = \text{proper velocity (mixed quantity)}$$

ordinary velocity

$$\vec{u} = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} \vec{v}, \quad \eta^\mu = \frac{dx^\mu}{d\tau} \text{ proper 4-velocity}$$

if $\tau = 89.58 \times 10^{-12}$ second (life time of K_S^0 meson)

$$c\tau = 3 \times 10^8 \text{ m/sec} \times 89.58 \times 10^{-12} \text{ sec}$$

$$= 2.68 \text{ cm}$$

Is mean life time a lab variable or a proper time variable?

$$\tau = \frac{1}{\Gamma} = \frac{1}{1 \text{ MeV}} = 10^{-6} (\text{eV})^{-1}$$

<u>1 TeV</u>	1 GeV	$\approx 3.56 \text{ as } 10^{-18}$	3560 as	1068 m	1068 km
	1 MeV	$\approx 3.56 \text{ fs } 10^{-15}$		106.8 cm	
	1 KeV	$\approx 3.56 \text{ ps } 10^{-12}$		0.1068 cm	
	1 eV	$\approx 3.56 \text{ ns } 10^{-9}$		1.068 μm	
	0.001 eV	$\approx 3.56 \text{ \mu\text{s} } 10^{-6}$		1.068 mm	
Γ	τ	$c\tau$			

$$J^{\pm}, 356 \text{ ps}, 10.68 \text{ cm}$$